# **Studies on Some Titanium-Substituted Fe<sub>2</sub>MoO<sub>4</sub> Spinel Oxides**

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Electrical resistivity  $(\rho)$  and thermoelectric power  $(\alpha)$  measurements were carried out in inert atmosphere on  $Fe<sub>2</sub>Mo<sub>1-x</sub>$  $Ti_xO_4$  (0.0  $\leq$  *x*  $\leq$  1.0) spinel oxides in the temperature ranges 100**–**600 and 300**–**600K, respectively. Thermal activation energy (*E*a), carrier concentration (n), activation energy for carrier concentration generation  $(E_n)$ , and mobility  $(\mu)$  values have been calculated from resistivity and thermoelectric power data. The results show that conduction in titanium-substituted  $Fe<sub>2</sub>MoO<sub>4</sub>$ samples, i.e.,  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$ , is carried out through the hopping of charge carriers, and the linear  $\ln(\rho)$  vs  $1/T$  plots show a break at the magnetic phase transition temperature. Progressive substitution of molybdenum by titanium in  $Fe<sub>2</sub>MoO<sub>4</sub>$  shows that the ratio of  $Fe^{3+}/Fe^{2+}$  decreases and in  $Fe_2TiO_4$  the ratio is very small. The decrease in the amount of  $Fe<sup>3+</sup>$  with increasing *x* results in the high resistivity and large lattice parameter of  $Fe<sub>2</sub>TiO<sub>4</sub>$ .  $\circ$  1998 Academic Press

## INTRODUCTION

 $Fe<sub>2</sub>MoO<sub>4</sub>$  is a cubic spinel showing some very interesting magnetic properties and has been studied by various groups for the past three decades (1*—*[7\)](#page-5-0). The most controversial point in all these studies has been the valence state of the cations and their distribution between the tetrahedral and octahedral sites of the spinel lattice. Studies by [Ramdani](#page-5-0) *[et](#page-5-0) [al](#page-5-0)*. (8) and [Domenichini](#page-5-0) *et al*. (9) have shown that the cations present in the ferrite are  $Fe^{2+}$ ,  $Fe^{3+}$ ,  $Mo^{3+}$ , and Mo<sup>4+</sup> and the formal valence assignment can be best represented by the equilibrium reactions [\(8\)](#page-5-0)

$$
Fe_B^{2+} + Fe_A^{3+} + Mo^{3+} = Fe_B^{3+} + Fe_A^{2+} + Mo^{3+} = Fe_B^{2+} + Fe_A^{2+} + Mo^{4+}.
$$

Recently, Roy *[et al](#page-5-0)*. (10) carried out some magnetic measurements on titanium-substituted  $Fe<sub>2</sub>MoO<sub>4</sub>$ urements on titanium-substituted  $Fe<sub>2</sub>MoO<sub>4</sub>$ , i.e.,  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$  samples. The results confirmed the presence of  $Fe<sup>2+</sup>$  and  $Fe<sup>3+</sup>$  ions in the ferrites.

The present work was taken up to study the effect of titanium substitution on the electrical transport properties of  $Fe<sub>2</sub>MoO<sub>4</sub>$ .

#### EXPERIMENTAL

Solid solutions of  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$  ( $x = 0.0, 0.2, 0.4,$  0.6, 0.8, and 1.0) were prepared by thoroughly mixing stoichiometric amounts of Fe<sub>2</sub>O<sub>3</sub> (specpure, Johnson– Mathey), Fe (electrolytic grade, Sarabhai Chemicals),  $MoO<sub>2</sub>$  (reduced from specpure  $MoO<sub>3</sub>$ ), and  $TiO<sub>2</sub>$  (analytic grade, S.D. Fine chemicals) and grinding in an agate mortar for several hours. The samples in the pellet form were placed inside quartz tubes, which were then degassed under vaccum and sealed under  $10^{-5}$  Torr. The sealed tubes were heated to 1170*°*C for 2h and then quenched in liquid nitrogen.

X-ray diffraction analyses of all the samples ( $x = 0.0$  to 1.0) were carried out in a Philips X-ray diffraction unit (Model PW-1710) using Cu*K* $\alpha$  radiation ( $\lambda = 1.5418$ Å) with Ni filter.

Resistivity measurements were carried out by four-probe technique in an inert atmosphere in the temperature range 100*—*600 K using silver paste for ohmic contact. Thermoelectric power measurements of all the polycrystalline samples were carried out in argon atmosphere in the temperature range 300*—*600K following the procedure described elsewhere [\(11\)](#page-5-0). The samples were heated at a rate of 200*°*C/h to avoid any phase separation during the measurements [\(8\).](#page-5-0)

#### RESULTS AND DISCUSSION

[Figure 1](#page-1-0) shows the plot of lattice parameter a and the ferrimagnetic Curie temperature  $T_c$  against the titanium content of the  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$  solid solution samples. With increasing *x*, the lattice parameter a increases linearly following Vegard's law. Such a change in the lattice parameter was also observed by Abe *et al*[.](#page-5-0) [\(12\)](#page-5-0). The Curie temperature however shows a gradual decrease as the molybdenum content in the ferrite is reduced.

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<span id="page-1-0"></span>

FIG. 1. Plots of *a* and  $T_c$  vs *x* for the Fe<sub>2</sub>Mo<sub>1-*x*</sub>Ti<sub>*x*</sub>O<sub>4</sub> samples.

An increase in the lattice parameter (Fig. 1) with the substitution of  $Mo^{4+}$  by  $Ti^{4+}$  is rather surprising since the size of  $Mo^{4+}$  (65 pm) is larger than the size of the substituting ion,  $Ti^{4+}$  (60.5 pm). Earlier studies have shown that in  $Fe<sub>2</sub>MoO<sub>4</sub>$ , molybdenum is present both in the trivalent  $(Mo<sup>3+</sup>)$  and tetravalent  $(Mo<sup>4+</sup>)$  states and consequently, for oxygen stoichiometry, iron is present in the divalent and trivalent states, i.e.,  $Fe^{2+}$  and  $Fe^{3+}$ . This implies that when molybdenum is substituted by titanium the amount of  $Fe<sup>3+</sup>$ in the ferrite is reduced. Thus, substitution of Mo by  $Ti<sup>4+</sup>$  effectively leads to the replacement of Fe<sup>3+</sup> (55pm) by Fe<sup>2+</sup> (78 pm); i.e., a smaller  $Fe^{3+}$  ion is replaced by a larger  $Fe<sup>2+</sup>$  ion, and so the lattice parameter of  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$  samples is expected to increase with increasing *x*, which is actually shown in the results in Fig. 1.

Figure 2 shows the room temperature resistivity vs composition plot of  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$  samples. The results show that up to  $x = 0.6$ , the resistivity increases very slightly, but on further increase of *x*, the resistivity of the samples increases by almost two orders of magnitude. This is expected since substitution leads to a decrease in the  $Fe^{3+}/Fe^{2+}$ ratio, and as will be discussed later, this leads to a decrease in the number of charge carriers.

The results of the temperature variation of resistivity show linear plots of  $\ln(\rho)$  vs  $1/T$  for all samples between 300 and 600K. The plots at lower temperatures however show slight deviation from linearity [\(Figs 5](#page-3-0) and [6](#page-4-0)). Using Arrhenius equation

$$
\rho = \rho_0 \exp\left[E_a / kT\right] \tag{1}
$$

(where  $\rho$  is the resistivity, T is the absolute temperature,  $k$  is the Boltzmann constant, and  $E_a$  is the thermal activation energy), the  $E_a$  values were calculated from the linear plots, which are given in [Table](#page-2-0) [1](#page-2-0). The chemical composition of various titanium-substituted  $Fe<sub>2</sub>MoO<sub>4</sub>$  samples and their code names are also given in Table 1. Similar to the reported values [\(8,13\)](#page-5-0), the  $E_a$  values of  $Fe_2MoO_4$  and  $Fe_2TiO_4$  are very small, implying hopping conduction in these ferrites.

In order to confirm hopping conduction in these ferrities,  $ln(\rho/T)$  was plotted against 1/T. [Figures 3](#page-2-0) and [4](#page-3-0) show the  $ln(\rho/T)$  vs  $1/T$  plots in the temperature range 300–600 K. As is expected in semiconductors with hopping conduction, all the plots were found to be linear. However, the plot of FTM6 shows that between 400 and 476K the resistivity remains almost constant. On repeating the measurements, reproducible results were obtained [\(Fig. 3,](#page-2-0) inset). Further studies on FTM6 must be carried out to explain this anomalous result.



FIG. 2. Plots of room temperature resistivity  $\rho$  vs *x* for the Fe<sub>2</sub> Ti*x*<sup>O</sup><sup>4</sup> samples.

<span id="page-2-0"></span>TABLE 1 Sample Composition, Code Name, Thermal Activation Energy  $(E_a)$ , Optical Phonon Frequency  $(\gamma_0)$ , and Mobility  $(\mu)$  at 550 K for Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub> Samples

Sample composition	Code name $300-573$ K	$E_a$ (eV)	$\gamma_0 \times 10^{11}$ $(\sec^{-1})$	$\mu_{550\,\mathrm{K}}$ $\rm (cm^2 V^{-1} sec^{-1})$
Fe <sub>2</sub> MoO <sub>4</sub>	FTM10	0.052	0.89	$2.68 \times 10^{-4}$
$Fe2Mo0$ <sub>8</sub> $Ti0$ <sub>2</sub> $O4$	FTM8	0.127	4.00	$2.90 \times 10^{-4}$
$Fe2 Mo0.6 Ti0.4 O4$	FTM6	0.103	1.91	$3.00 \times 10^{-4}$
$Fe2Mo0.4Ti0.6O4$	FTM4	0.133	1.65	$1.23 \times 10^{-4}$
$Fe2 Mo0$ , $Ti0$ , $O4$	FTM2	0.165	0.16	$6.82 \times 10^{-6}$
Fe <sub>2</sub> TiO <sub>4</sub>	FTM0	0.250	0.11	$8.50 \times 10^{-7}$

Studies on Fe<sub>2</sub>MoO<sub>4</sub> by [Ramdani](#page-5-0) *et al.* (8) have shown that the ferrite is a semiconductor in which conduction is carried out through the hopping of charge carriers between  $Fe<sup>2+</sup> – Fe<sup>3+</sup>$  and  $Mo<sup>3+</sup> – Mo<sup>4+</sup>$ . During substitution of Mo by Ti in the solid solutions,  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$ , the amounts of both Mo3*`* and Fe3*`* are likely to be reduced and hence with increasing *x*, resistivity should increase. The results in [Fig. 2](#page-1-0) show this increase, which indirectly confirms the presence of  $Fe^{3+}$  and  $Mo^{3+}$  in  $Fe_2MoQ_4$ . It also shows a sudden increase in resistivity between FTM4 and FTM2. Spinel oxides usually show hopping conduction, and the hopping of charge carriers can occur between (i) tetrahedral sites, (ii) octahedral sites, and (iii) tetrahedral and octahedral sites of the spinel lattice. The contribution from (i) and (iii) toward the total conduction of the spinel may be neglected, because the distance between two adjacent tetrahedral sites is larger than that between two adjacent octahedral sites and the hopping between two crystallographically nonequivalent sites is energetically unfavorable [\(14\)](#page-5-0). However, [Ramdani](#page-5-0) *et al.* (8) have suggested that in  $Fe<sub>2</sub>MoO<sub>4</sub>$ , the low resistivity can be explained by taking the hopping of charge carriers between the tetrahedral sites into consideration. Thus, during substitution of Mo by Ti as the  $Fe<sup>3+</sup>$  content decreases, the probability of hopping of charge carriers between  $Fe<sup>2+</sup><sub>tet</sub>$  and  $Fe<sup>3+</sup><sub>det</sub>$  becomes smaller and on going from FTM4 to FTM2 the contribution from tetrahedral site hopping becomes negligible, and this is manifest in the sharp rise in the room temperature resistivity between FTM4 and FTM2.

The plot of  $Fe<sub>2</sub>MO<sub>4</sub>$ , (Fig. 3a) shows a break near 400 K which is its magnetic phase transition temperature  $T_c$ . Similar results have been reported by Ramdani *et al*. (8). Breaks in the plots of  $\ln(\rho)$  vs  $1/T$  were also observed near the magnetic phase transition temperature of the substituted samples [\(Figs. 5](#page-3-0) and [6\)](#page-4-0).

Taking the best fit of the linear plot of  $\ln(\rho/T)$  vs  $1/T$ (Figs. 3 and [4\)](#page-3-0), the optical phonon frequency ( $\gamma_0$ ) and mobility values  $(\mu)$  at different temperatures were calculated following the method of [Metselaar](#page-5-0) *et al*. (15). The values are given in Table 1. The values of the optical phonon frequency  $(y_0)$  confirm hopping conduction in these samples. The values of mobility,  $\mu$ , show a decrease with increasing  $x$ . This is expected, since both  $Fe<sup>3+</sup>$  and Mo<sup>3+</sup> are removed by titanium substitution, which implies that the number of hopping centers is reduced and as a consequence the distance through which the charge carrier can hop is increased, resulting in a decrease in the mobility.

The results of the thermoelectric power measurements show that all the samples are p-type and the magnitude of



FIG. 3. Plots of  $\ln(\rho/T)$  vs  $1/T$  for (a) FTM10, (b) FTM8, and (c) FTM6. (Inset) Repeat plot of FTM6.

<span id="page-3-0"></span>

FIG. 4. Plots of  $\ln(\rho/T)$  vs  $1/T$  for (a) FTM4, (b) FTM2, and (c) FTM0.

Seebeck coefficient  $(x)$  decreases with increasing temperature. From the values of  $\alpha$ , the values of carrier concentration n were calculated using

$$
n = N_{\nu} \exp(-\alpha/k), \tag{2}
$$

where  $N_{\nu}$  is the density of states involved in the conduction process and  $k$  is the Boltzmann constant.  $N_{v}$  values were calculated following the method of [Metselaar](#page-5-0) *et al*. (15). The values of **n** are shown in [Table 2](#page-5-0) for all the  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>$ values of **n** are shown in Table 2 for all the  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$ <br>samples. From the results it is apparent that with increasing *x*, there is a decrease in the number of charge carriers. These results support the suggestions made earlier, that substitution of Mo by Ti leads to a decrease in the  $Fe^{3+}/Fe^{2+}$  ratio.

From the slope of the  $ln(n)$  vs  $1/T$  plots in the temperature range 370–600 K [\(Fig. 7\)](#page-4-0),  $E_n$  was calculated and the values are given in [Table 2.](#page-5-0) In order to ascertain the conduction mechanism in these samples,  $E_n$  values were compared with  $E_a$  values. For all samples  $E_a > E_n$ , which is expected when conduction is by hopping of charge carriers ([16\)](#page-5-0). These results thus confirm that as in  $Fe<sub>2</sub>MoO<sub>4</sub>$ , in the  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$  samples also conduction appears to be by the hopping of charge carriers between  $Fe^{3+}$  and  $Fe^{2+}$  ions.



FIG. 5. Plots of  $ln(\rho)$  vs  $1/T$  for (a) FTM10 and (b) FTM8.

<span id="page-4-0"></span>

FIG. 6. Plots of  $ln(\rho)$  vs  $1/T$  for (a) FTM6, (b) FTM4, and (c) FTM2.

For small polaron conduction, the Seebeck coefficient for the thermoelectric power is given by [\(17\)](#page-5-0)

$$
\alpha = \frac{k}{e} \left[ \ln \beta \, \frac{\left[ \text{Fe}_{\text{oct}}^{3+} \right]}{\left[ \text{Fe}_{\text{oct}}^{2+} \right]} + A \right]. \tag{3}
$$

In all the samples under investigation a small activation energy of thermoelectric power is consistent with the small polaron hopping mechanism. Thus, using Eq. [3], the ratio of  $[Fe<sub>oct</sub><sup>3+</sup>]/[Fe<sub>oct</sub><sup>2+</sup>]$  was calculated taking the value of  $\beta = 2$ 

and neglecting the value of *A* as was suggested by [Chang](#page-5-0) *et al*[. \(13\)](#page-5-0) and [Tuller](#page-5-0) *et al*. (18); the values are given in [Table](#page-5-0) [2.](#page-5-0) The results in [Table](#page-5-0) [2](#page-5-0) show that the ratio decreases as molybdenum is progressively replaced by titanium, and in  $Fe<sub>2</sub> TiO<sub>4</sub>$ , the ratio is very small. These results again confirm that substitution of Mo by Ti in  $Fe<sub>2</sub>MoO<sub>4</sub>$  reduces the amount of  $Fe<sup>3+</sup>$  in the ferrite.

From these results the following cation distributions for Fe<sub>2</sub>MoO<sub>4</sub> and Fe<sub>2</sub>TiO<sub>4</sub> may be suggested: Fe<sub>0,737</sub>Fe<sub>0,763</sub><br>[Fe<sub>0,737</sub>Fe<sub>0,263</sub>Mo<sub>0,526</sub>Mo<sub>0,474</sub>]O<sub>4</sub> and Fe<sub>0,965</sub>Fe<sub>0,035</sub><br>[Fe<sub>0,965</sub>Fe<sub>0,035</sub>Ti<sup>4+</sup>]O<sub>4,035</sub>.



FIG. 7. Plots of  $\ln(n)$  vs  $1/T$  for  $Fe_2Mo_{1-x}Ti_xO_4$  samples.

TABLE 2

<span id="page-5-0"></span>Charge Carrier Concentration (*n*), Activation Energy for Charge Carrier Generation (*En*), and Octahedral Iron Valence Ratio ([Fe<sup>3+</sup>]/[Fe<sup>2+</sup>]) for Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub> Samples

Code name	$\mathbf{n} \times 10^{22}$ 300K	$E_n$ (eV) $370 - 573$ K	$E_a - E_n$ (eV)	$[Feoct3+1]/[Feoct2+1]$ 300K
FTM10	3.70	0.013	0.039	0.357
FTM8	2.80	0.021	0.106	0.270
FTM6	2.09	0.047	0.056	0.202
FTM4	1.78	0.035	0.098	0.172
FTM2	1.36	0.048	0.117	0.131
FTM0	0.21	0.072	0.178	0.036

### **CONCLUSION**

From the results it may be concluded that similar to Fe<sub>2</sub>MoO<sub>4</sub>, all the titanium-substituted Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub> samples are p-type semiconductors in which conduction samples are p-type semiconductors in which conduction takes place by the hopping of charge carriers between Fe2*`—*  $Fe<sup>3+</sup>$  and between  $Mo<sup>3+</sup> – Mo<sup>4+</sup>$ . Near the ferrimagnetic to paramagnetic phase transition temperature,  $T_c$  all the  $Fe<sub>2</sub>Mo<sub>1-x</sub>Ti<sub>x</sub>O<sub>4</sub>$  samples show a change in slope in the ln( $\rho$ ) vs  $1/T$  plots. The substitution of molybdenum by titanium in  $Fe<sub>2</sub>MoO<sub>4</sub>$  results in a decrease in the charge carrier concentration,  $n$ , charge carrier mobility,  $\mu$ , and the ratio of  $[Fe<sub>oct</sub><sup>3+</sup>]/[Fe<sub>oct</sub><sup>2+</sup>].$  All these results confirm that both  $Fe<sup>3+</sup>$ and  $Fe^{2+}$  ions are present in  $Fe_2MoO_4$ , and in  $Fe_2TiO_4$ <br>a very small amount of  $Fe^{3+}$  appears to be present.

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